

Oleg B. Tarasov
NCSL / MSU, USA

Measurement of production cross sections and momentum distributions @ MSU

5th Fragment-Separator Experts Meeting
5th Fragment-Separator Experts Meeting

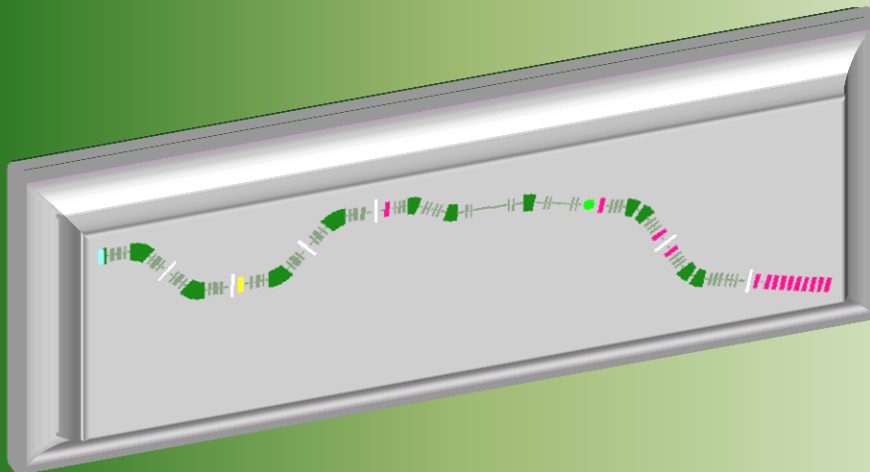
10-12 / 12 / 2013

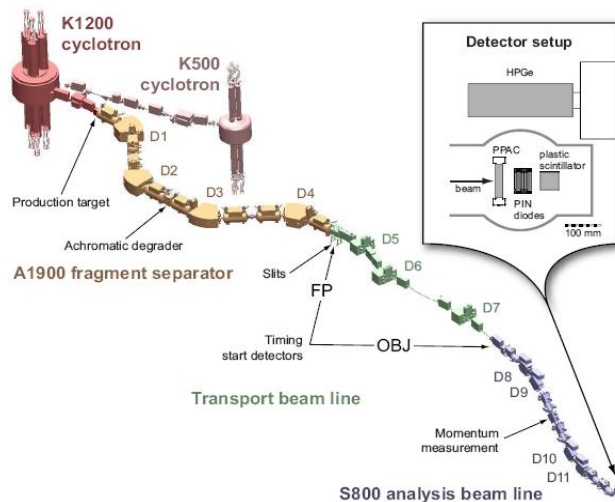
LISE++



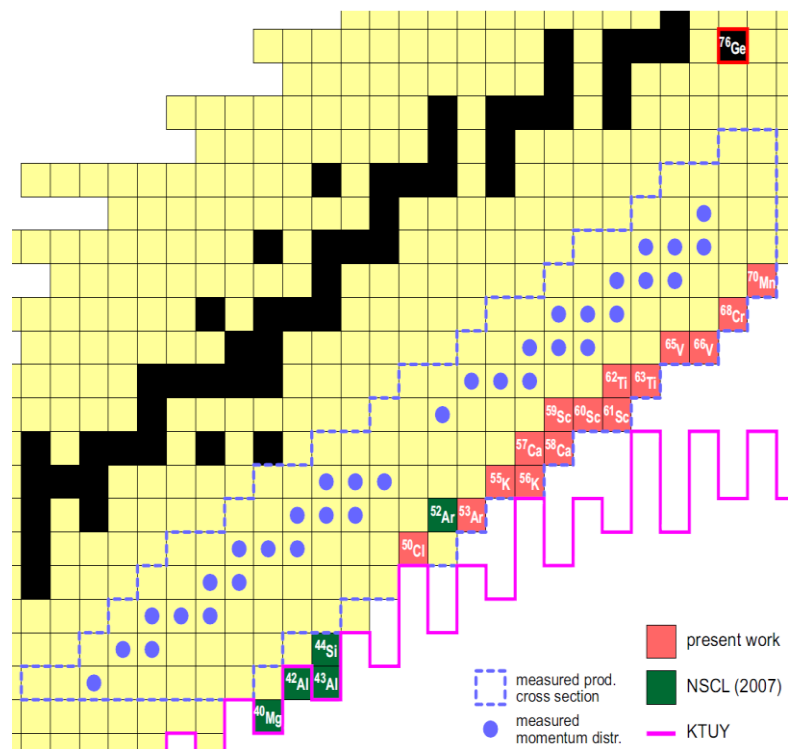
1. Introduction
2. Target thickness scanning approach to measure momentum distributions
3. Revision of target scanning approach
4. ^{76}Ge & ^{82}Se : momentum distributions
5. ^{76}Ge & ^{82}Se : cross sections
6. Isotope production close to the proton drip line
7. "Universal" model
8. Conclusion

LISE++





15 new isotopes of elements $17 \leq Z \leq 25$
 ^{50}Cl , ^{53}Ar , $^{55,56}\text{K}$, $^{57,58}\text{Ca}$, $^{59,60,61}\text{Sc}$,
 $^{62,63}\text{Ti}$, $^{65,66}\text{V}$, ^{68}Cr , ^{70}Mn



PRL **102**, 142501 (2009) PHYSICAL REVIEW LETTERS week ending 10 APRIL 2009

Evidence for a Change in the Nuclear Mass Surface with the Discovery of the Most Neutron-Rich Nuclei with $17 \leq Z \leq 25$

O. B.,^{1,2} D. J. Morrissey,^{1,3} A. M. Amthor,^{1,4} T. Baumann,¹ D. Bazin,¹ A. Gade,^{1,4} T. N. Ginter,¹ M. Hausmann,¹ N. Inabe,⁵ T. Kubo,⁵ A. Nettleton,^{1,4} J. Pereira,¹ M. Portillo,¹ B. M. Sherrill,^{1,4} A. Stolz,¹ and M. Thoennessen^{1,4}

¹National Superconducting Cyclotron Laboratory, Michigan State University, East Lansing, Michigan 48824, USA
²Flerov Laboratory of Nuclear Reactions, JINR, 141980 Dubna, Moscow Region, Russian Federation
³Department of Chemistry, Michigan State University, East Lansing, Michigan 48824, USA
⁴Department of Physics and Astronomy, Michigan State University, East Lansing, Michigan 48824, USA
⁵RIKEN Nishina Center, RIKEN, Wako-shi, Saitama 351-0198, Japan

Phys.Rev.Lett. 102, 142501 (2009) :

Phys.Rev.C. 80, 034609 (2009) :

NIM A 620, 578-584 (2010) :

New isotopes, Evidence for a Change in the Nuclear Mass Surface

Set-up, cross sections, momentum distributions

A new approach to measure momentum distributions

Beam	E (MeV/u)	I (pna)	N/Z
^{82}Se	139	35	1.412
^{76}Ge	130	20	1.375

$$\Delta N / \Delta Z = 2$$

^{64}Ti , ^{67}V , ^{69}Cr , ^{72}Mn
 ^{70}Cr 1event & ^{75}Fe 1event

Selected for a **Viewpoint** in *Physics*

PHYSICAL REVIEW C **87**, 054612 (2013)



Production cross sections from ^{82}Se fragmentation as indications of shell effects in neutron-rich isotopes close to the drip-line

O. B.,^{1,*} M. Portillo,² D. J. Morrissey,^{1,3} A. M. Amthor,² L. Bandura,² T. Baumann,¹ D. Bazin,¹ J. S. Berryman,¹ B. A. Brown,^{1,4} G. Chubarian,⁵ N. Fukuda,⁶ A. Gade,^{1,4} T. N. Ginter,¹ M. Hausmann,² N. Inabe,⁶ T. Kubo,⁶ J. Pereira,¹ B. M. Sherrill,^{1,4} A. Stolz,¹ C. Sumithrarachichi,¹ M. Thoennessen,^{1,4} and D. Weisshaar¹

¹National Superconducting Cyclotron Laboratory, Michigan State University, East Lansing, Michigan 48824, USA

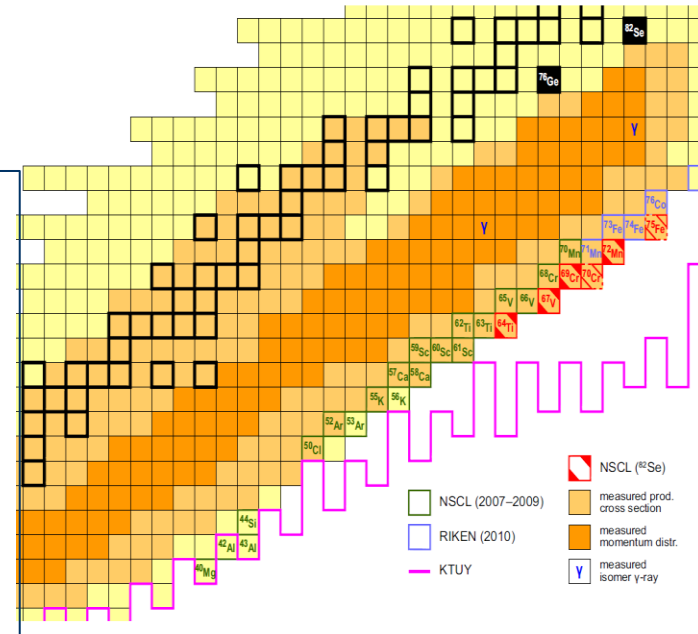
²Facility for Rare Isotope Beams, Michigan State University, East Lansing, Michigan 48824, USA

³Department of Chemistry, Michigan State University, East Lansing, Michigan 48824, USA

⁴Department of Physics and Astronomy, Michigan State University, East Lansing, Michigan 48824, USA

⁵Cyclotron Institute, Texas A&M University, College Station, Texas 77843, USA

⁶RIKEN Nishina Center, RIKEN, Wako-shi, Saitama 351-0198, Japan



Phys. Rev. C 87, 054612 (2013) : New isotopes, cross sections, momentum distributions, subshell closure at $N = 34$ around $Z = 20$

NIM A (2014) : momentum distribution measurement (detailed), revision of target thickness scanning approach to measure momentum distributions

New method:

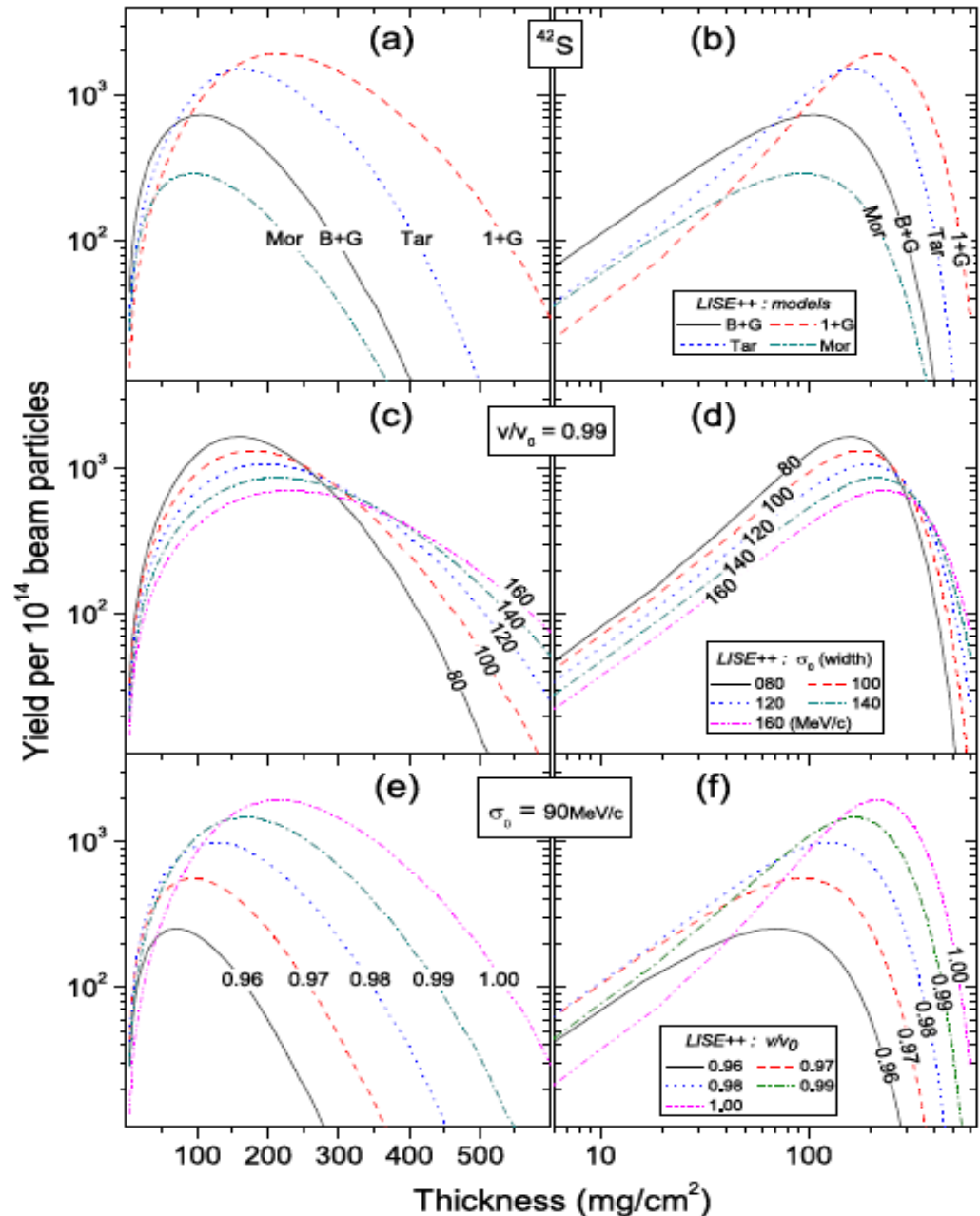
- Brho = const
- Target thickness variation

“Classic way:

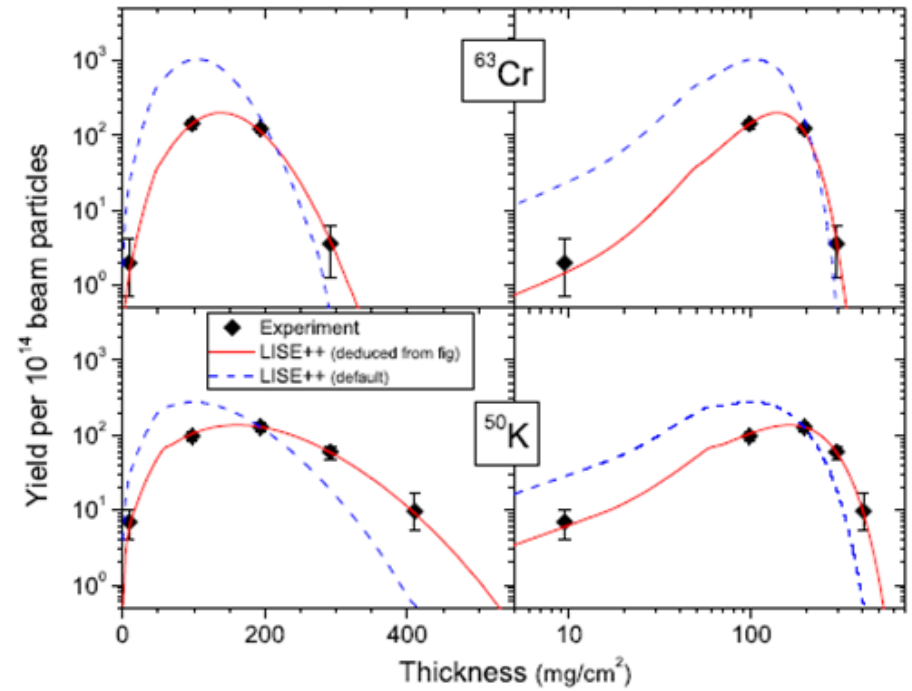
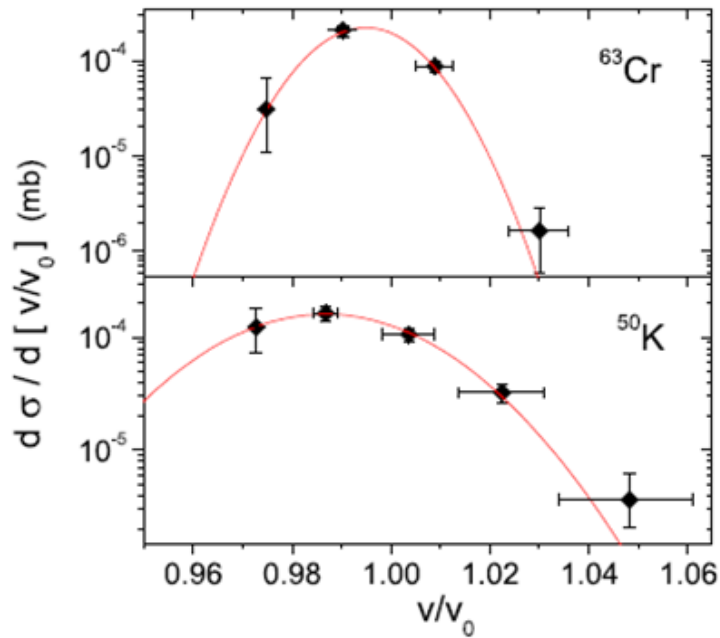
- Brho scanning
- thin target

A number of simulations have been carried out in order to illustrate the sensitivity of the momentum distribution characteristics to varying target thicknesses.

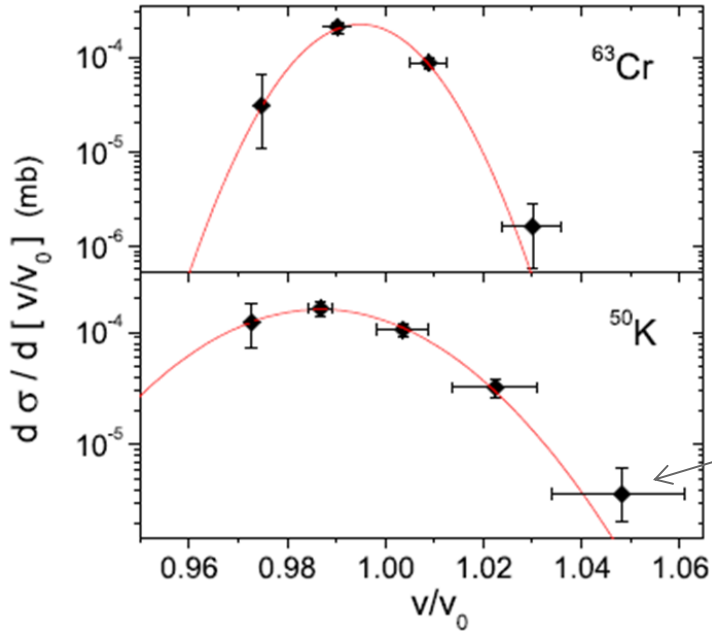
The rigidity of the last dipole was kept constant at 4.3 Tm while using the “Optimum target thickness” (thickness corresponding to maximum yield) routine to calculate production yields.



Run	Fragment of interest	Magnetic rigidity, $B\rho(Tm)$					Target mg/cm^2	Stripper mg/cm^2	Wedge, Kapton	$\Delta p/p$ (%)	Time <i>hour</i>
		$B\rho_{1,2}$	$B\rho_{3,4}$	$B\rho_{5,6,7}$	$B\rho_{8,9}$	$B\rho_{10,11}$					
1	^{43}S	4.3233	4.3233	4.3134	4.3036	4.3	Be 9.8	-	-	0.1	0.98
2							Be 97.5	-	-	0.1	2.03
3							Be 191	-	-	0.1	1.98
4							Be 288	-	-	0.1	1.85
5							Be 404	-	-	0.1	0.94



Characteristics	$B\rho$ scanning <i>Thickness = const</i>	Target scanning $B\rho = const$
Fragment separator tuning for each measurement	Yes	No
Particle identification for each measurement	At least should be verified	PID is constant
Number of measured distribution points	Large	Small
Number of measured isotopes	Large	Small
Measuring exotic nuclei (smallest cross-sections)	Difficult	Straight forward
Contribution of energy loss in thick targets	Small	Large
Extracting longitudinal momentum distributions	Straight forward	Difficult
Applicable energy region	No restrictions	Constant cross-section region

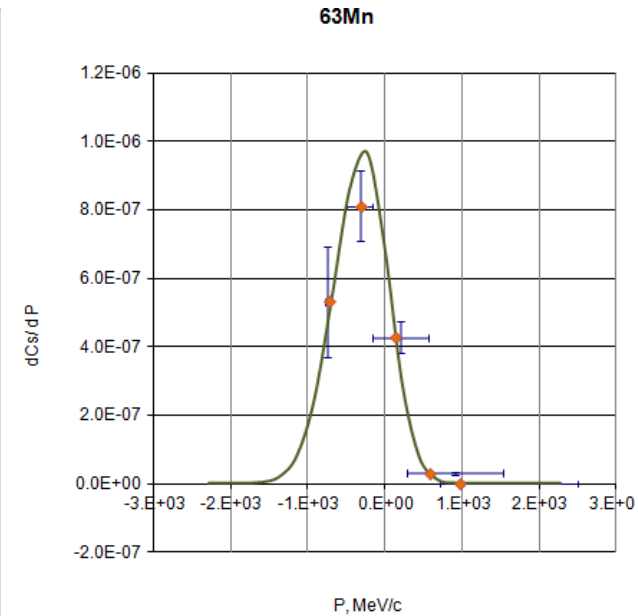
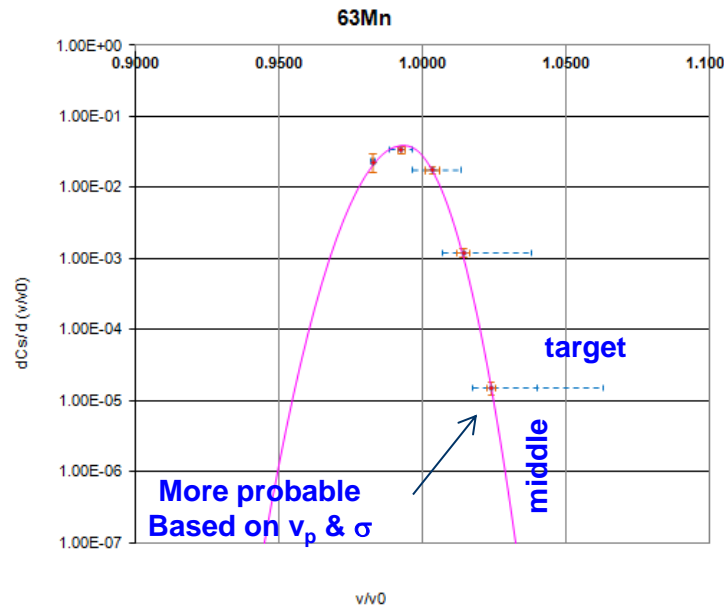


⁷⁶Ge : 5 targets (max 3 isotopes for one element)

⁸²Se : 7 targets (max 8 isotopes for one element)

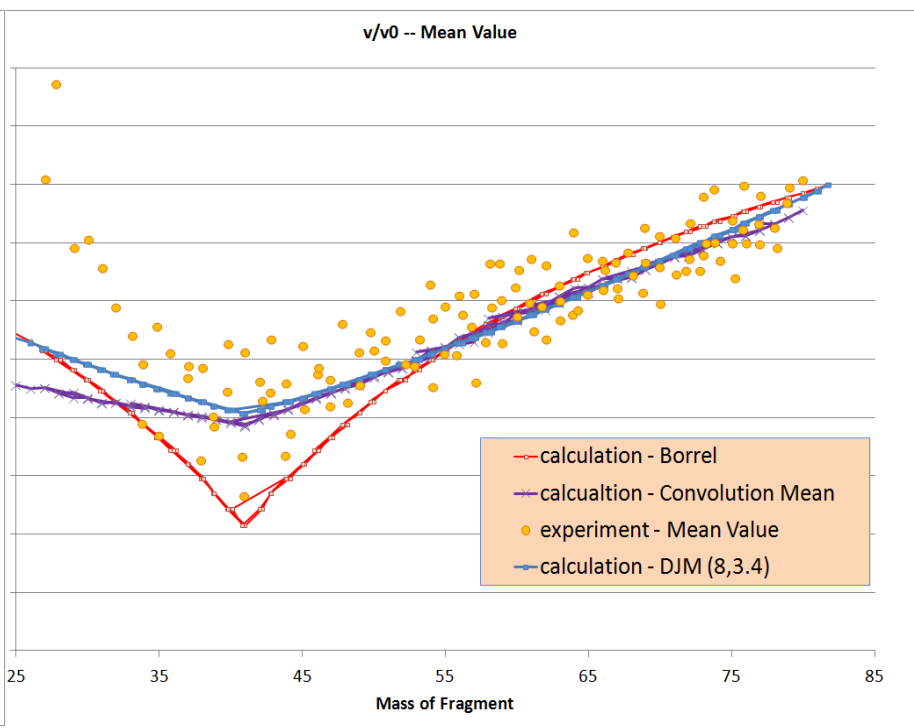
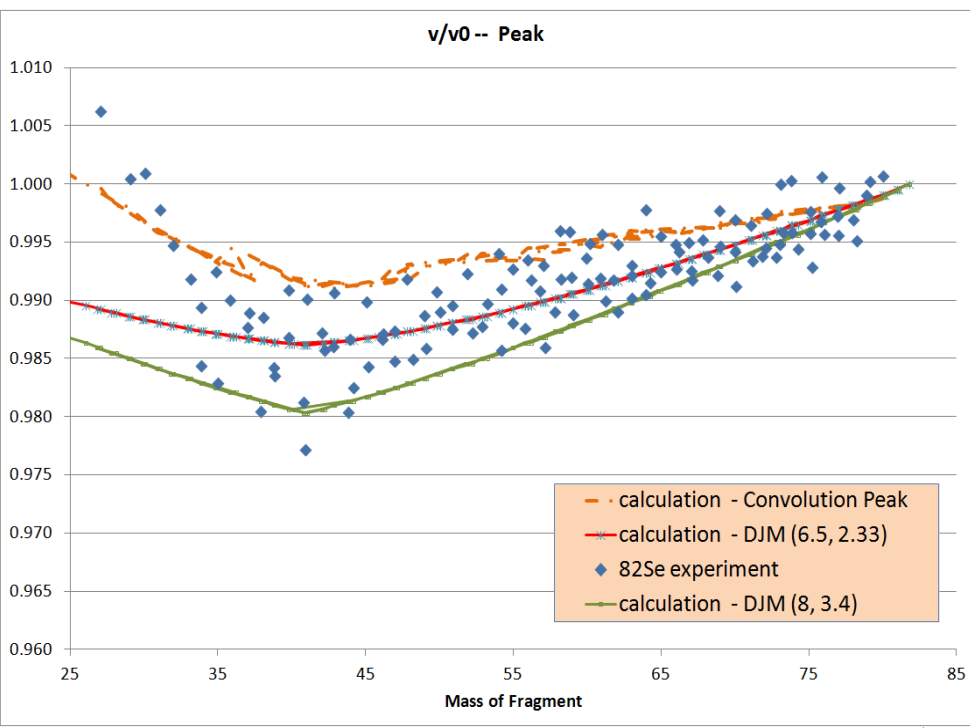
⁷⁶Ge analysis (2009) :
point for fit in the middle of target
or weights = const

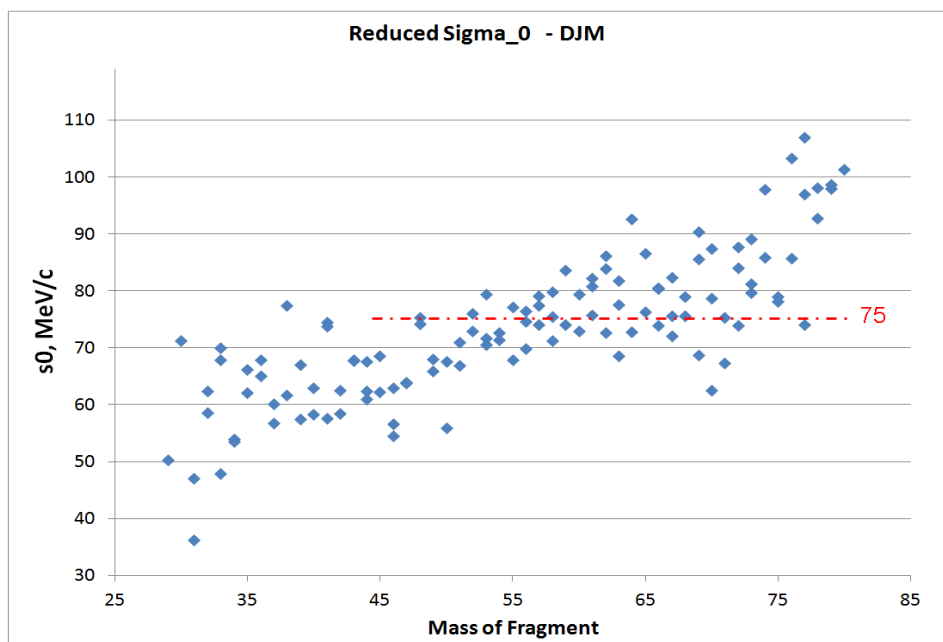
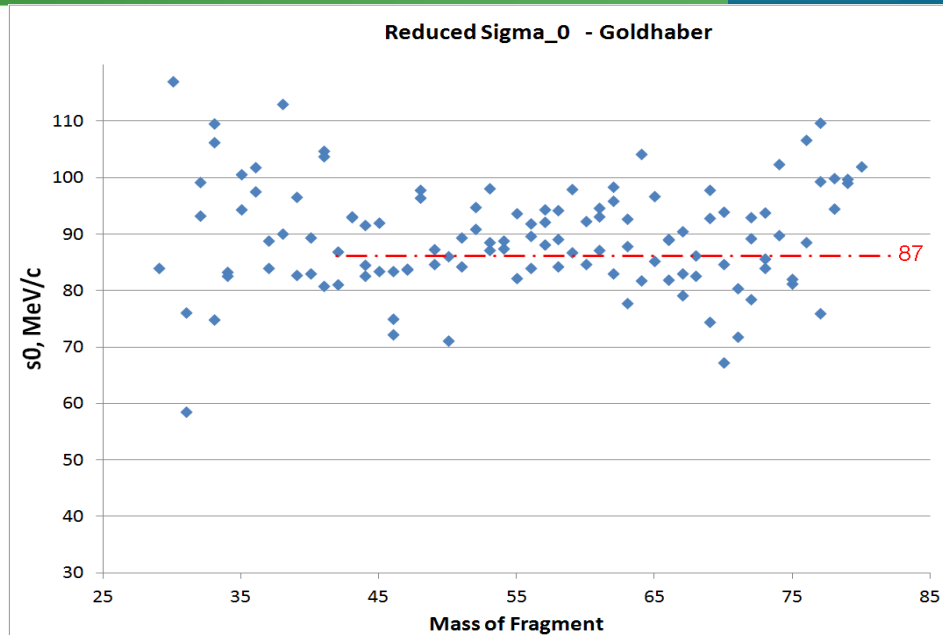
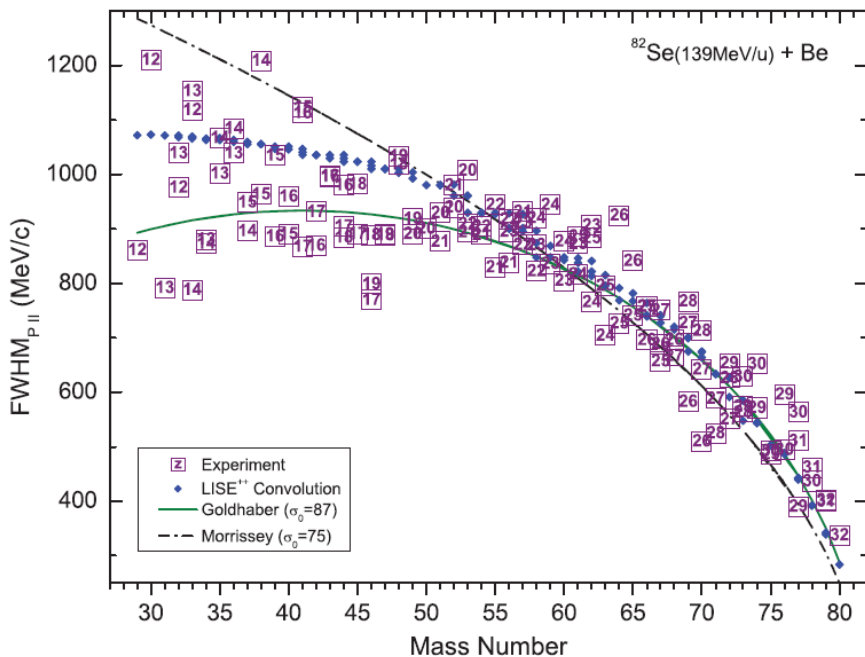
2012 update :
using weights $F(v_p, \sigma)$
from the momentum
distribution model
with v_p, σ ,



^{82}Se (139 MeV/u) + Be : Momentum Distributions – v/v_0

- Calculation - A [V.Borrel et al., Z.Pyhs.A314(1983)191] *Borrel*
- Calculation - B [F.Rami et al., NPA 444(1985)349]
- Calculation - C [O.Tarasov, NPA 734(2004)536] *convolution*
- Calculation - D [from two-body reaction]
- Calculation - E [D.Morrissey, PRC 39(1989)460] *DJM*





82Se(140.0 MeV/u) + Be -> 64Ti

Parallel momentum distribution

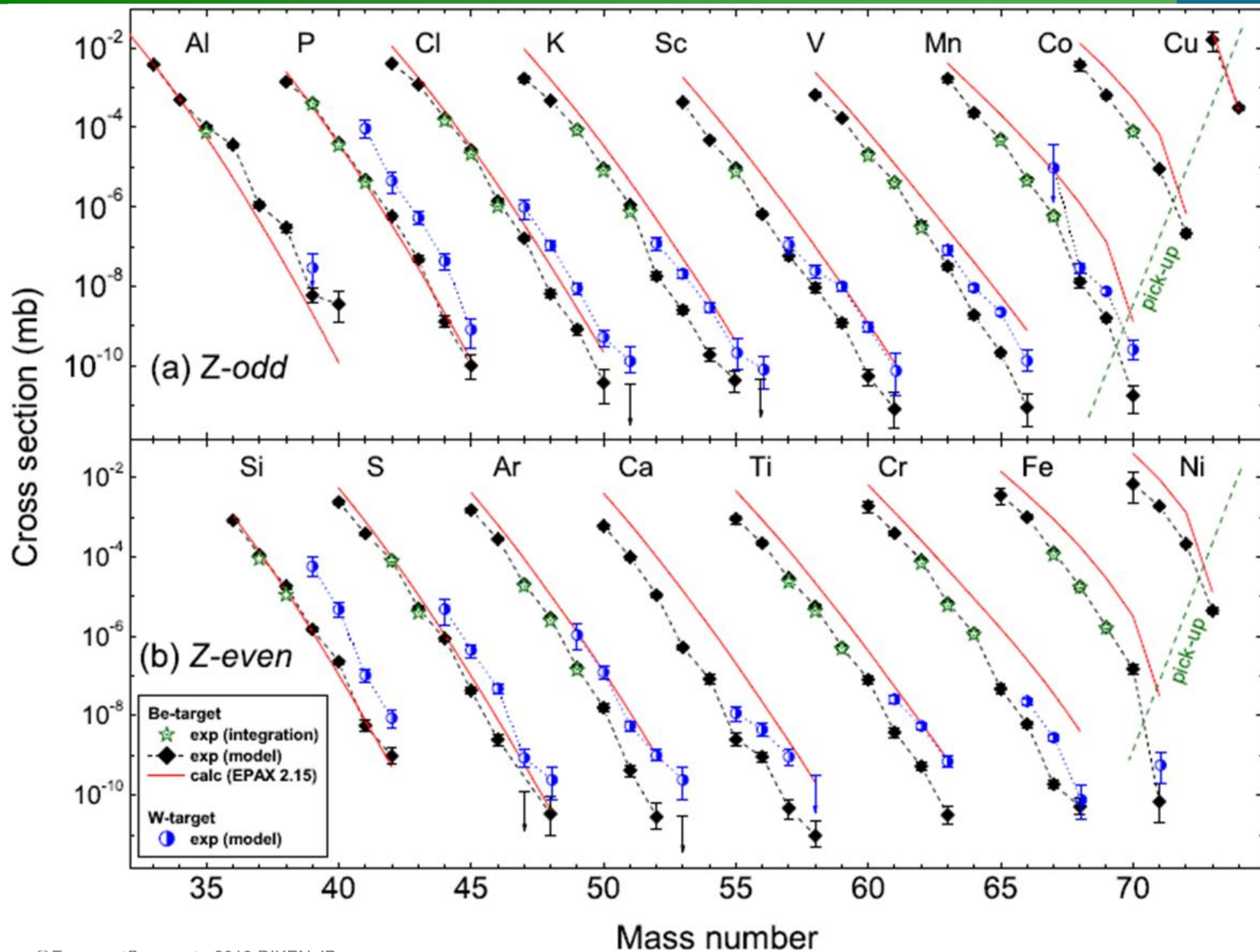
- [1] A.S.Goldhaber
Phys.Lett.B 53(1974)306
 $\sigma_{||}^2 = \sigma_0^2 \frac{A_F(A_p - A_F)}{A_2 - 1}$ $\sigma_0 = 87$ $\sigma_{||} = 327.5$
- [2] D.J.Morrissey
Phys.Rev.C 39(1989)460
 $\sigma_{||}^2 = \sigma_M^2 (A_p - A_F)$ $\sigma_M = 75$ $\sigma_{||} = 317.5$
- [3] W.A.Friedman
Phys.Rev.C 27(1983)569
 $\sigma_{||}^2 = \frac{\mu}{2x_0} \left[\frac{1+0.5y}{\sqrt{1+y}} + \frac{1}{\mu x_0} \right]$ settings $\sigma_{||} = 232.1$

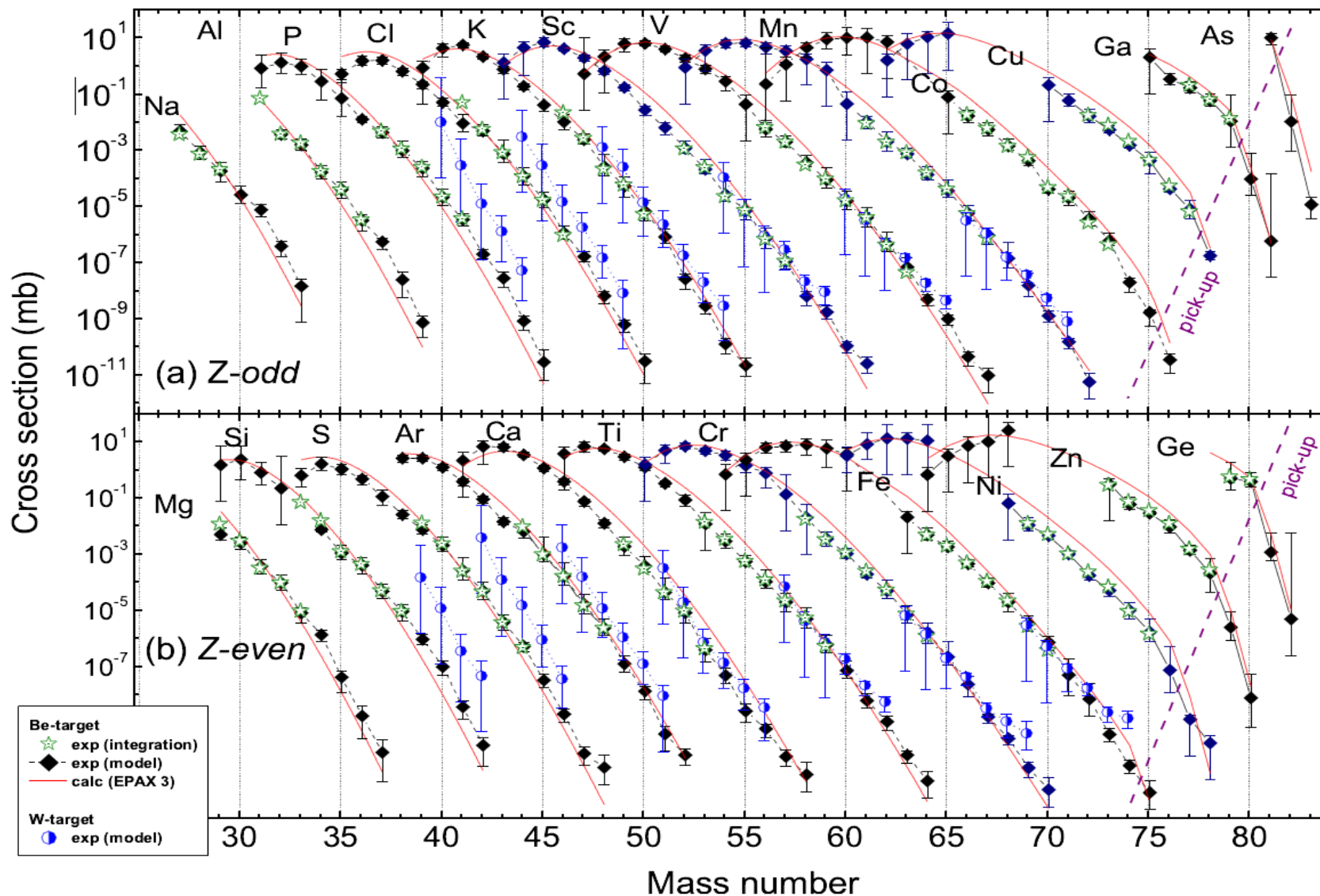
Asymmetry coefficient for Gaussian-like distributions [1-3] alpha (%) = 15 $\alpha = \frac{\sigma_{low}}{\sigma_{||}} - 1 = 1 - \frac{\sigma_{high}}{\sigma_{||}}$? Help

- [4] Universal parameterization (Convolution)
O.Tarasov, NPA 734(2004)536 settings $\sigma_0^{conv} = 91.5$ $\sigma_{||} = 343.0$

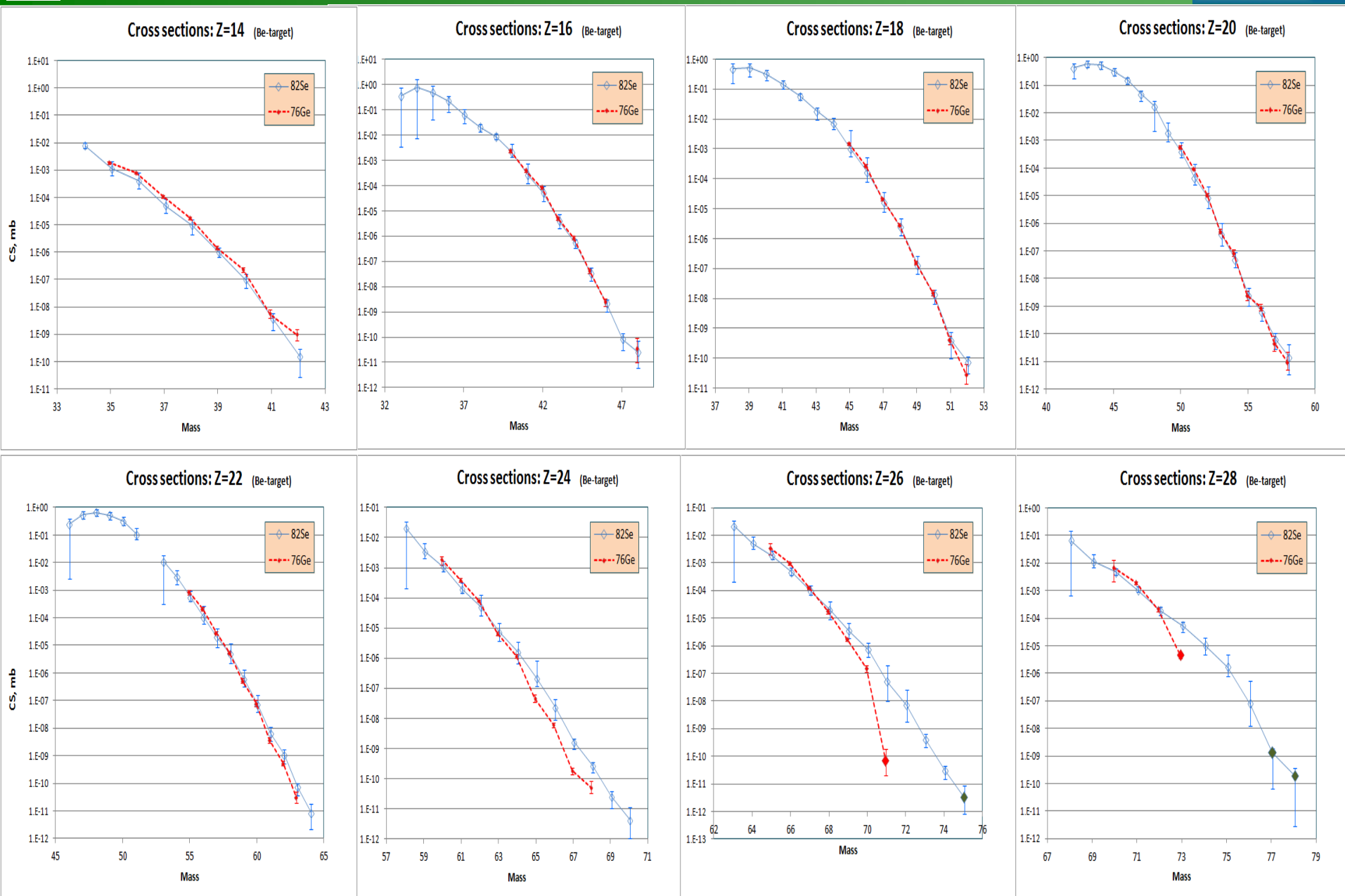
	82Se - asym	76Ge - new*	76Ge - old	default values
Number of isotopes	122	58	34	
velocity - DJM - peak	6.5 & 2.4			
velocity - DJM - mean	8 & 3.4	8 & 3.3	8 & 2.4	8 & 8
Velocity - Borrel (no fit, only for plot)	8	8		8
Average weighted				
GO_DJM	75 -11+9	73.1 ± 10.2	105 ± 15	86
GO_DJM * gamma		83.1		
GO_Goldhaber	87 -13+9	87.0 +- 7.9		90
GO_Goldhaber * gamma		98.9		

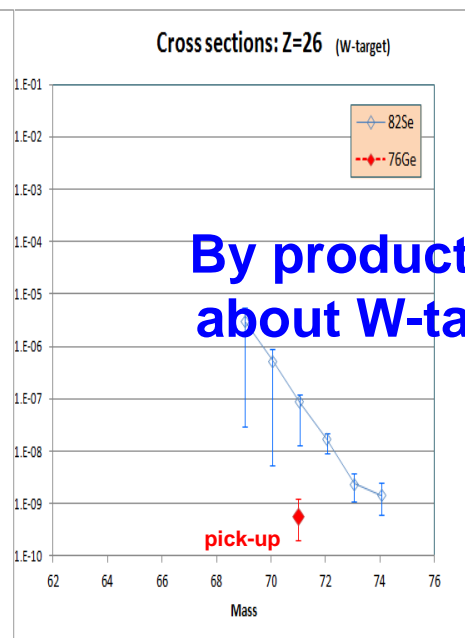
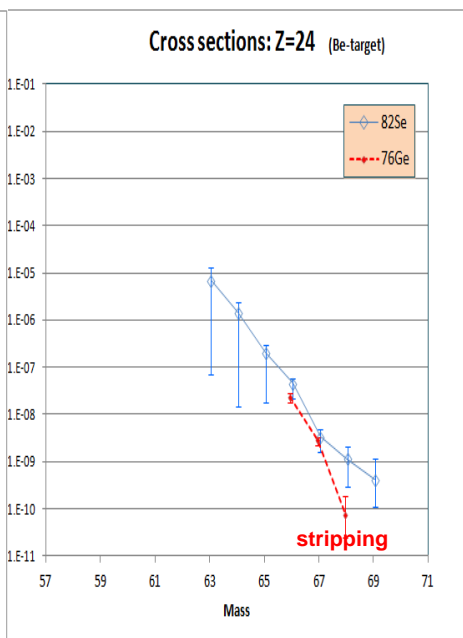
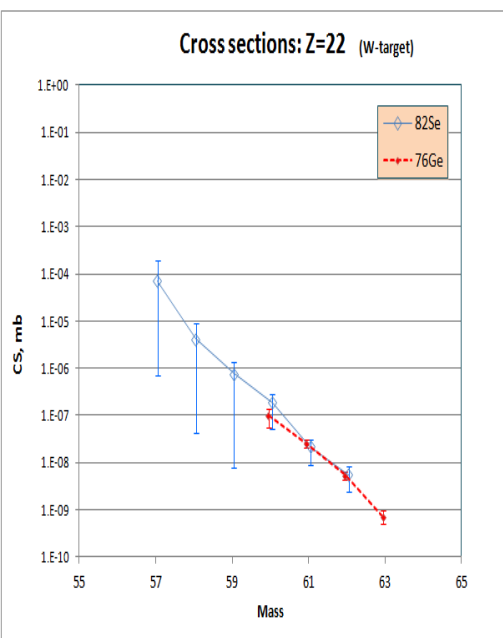
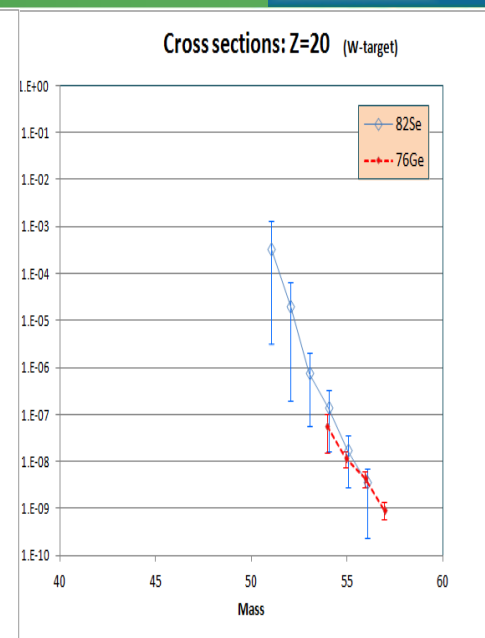
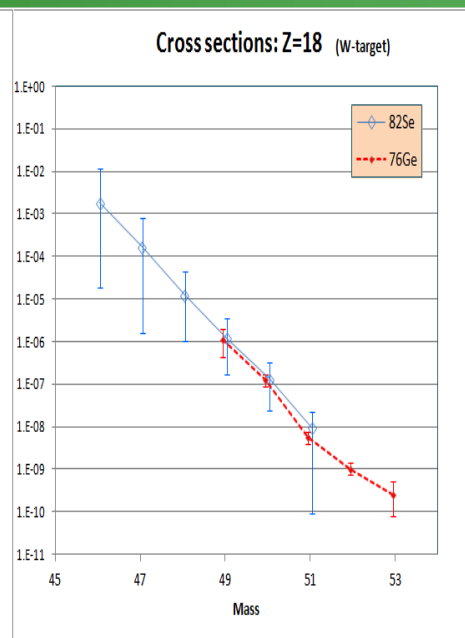
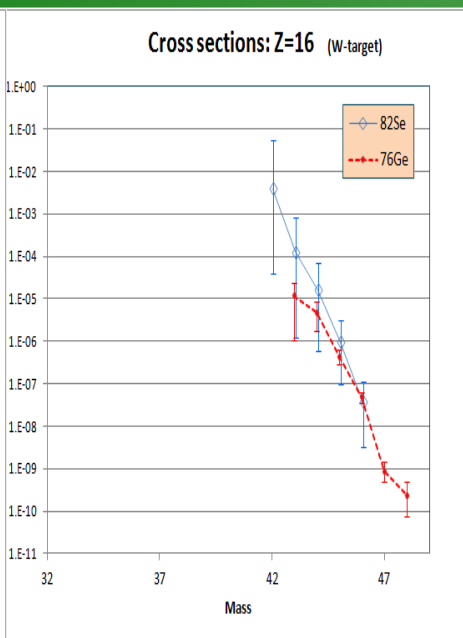
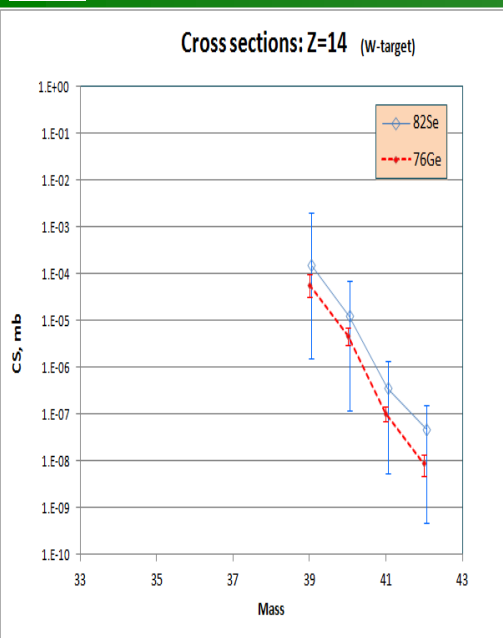
76Ge* -- target scanning re-analysis with weights use [February 17, 2012]



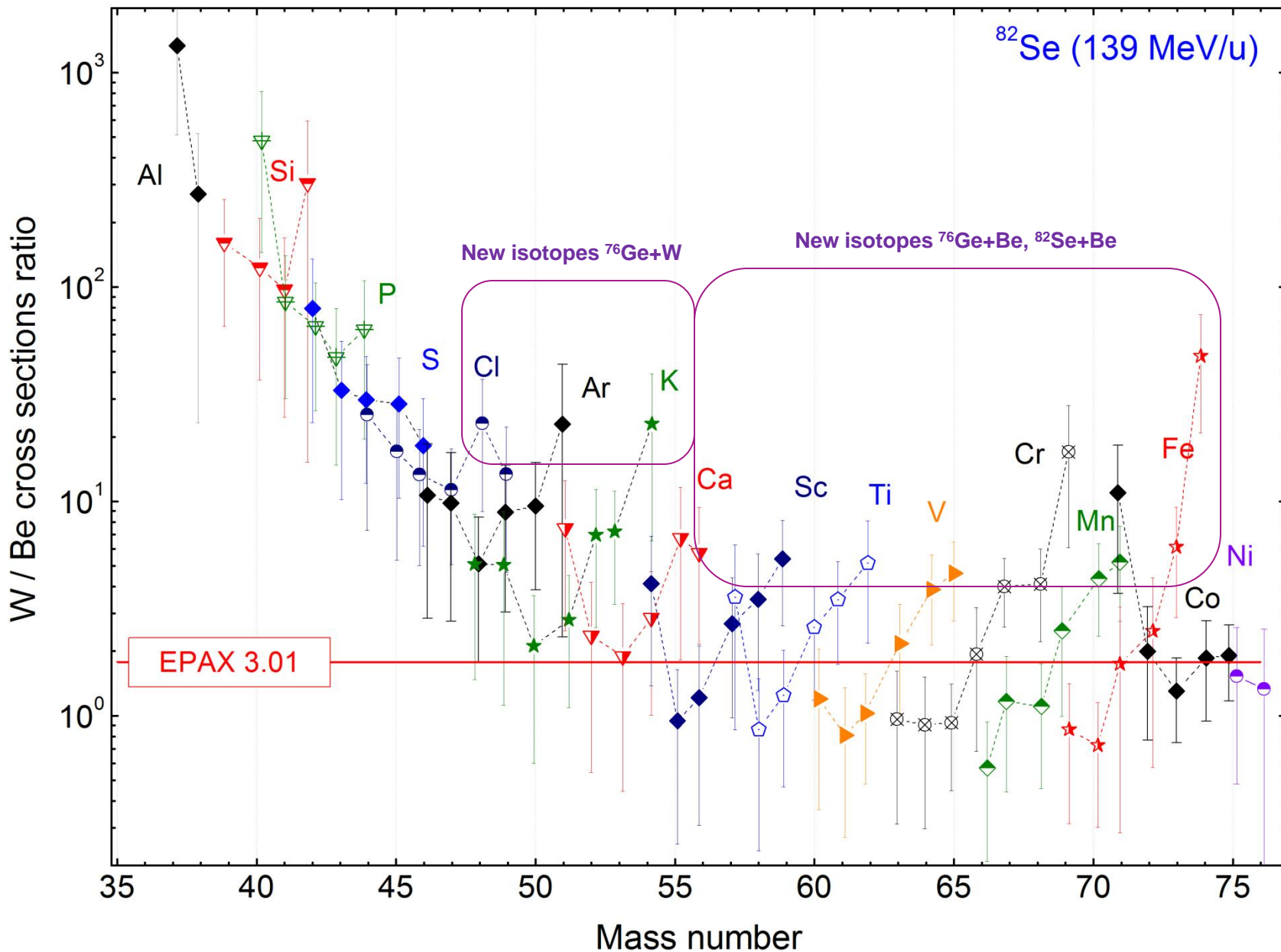


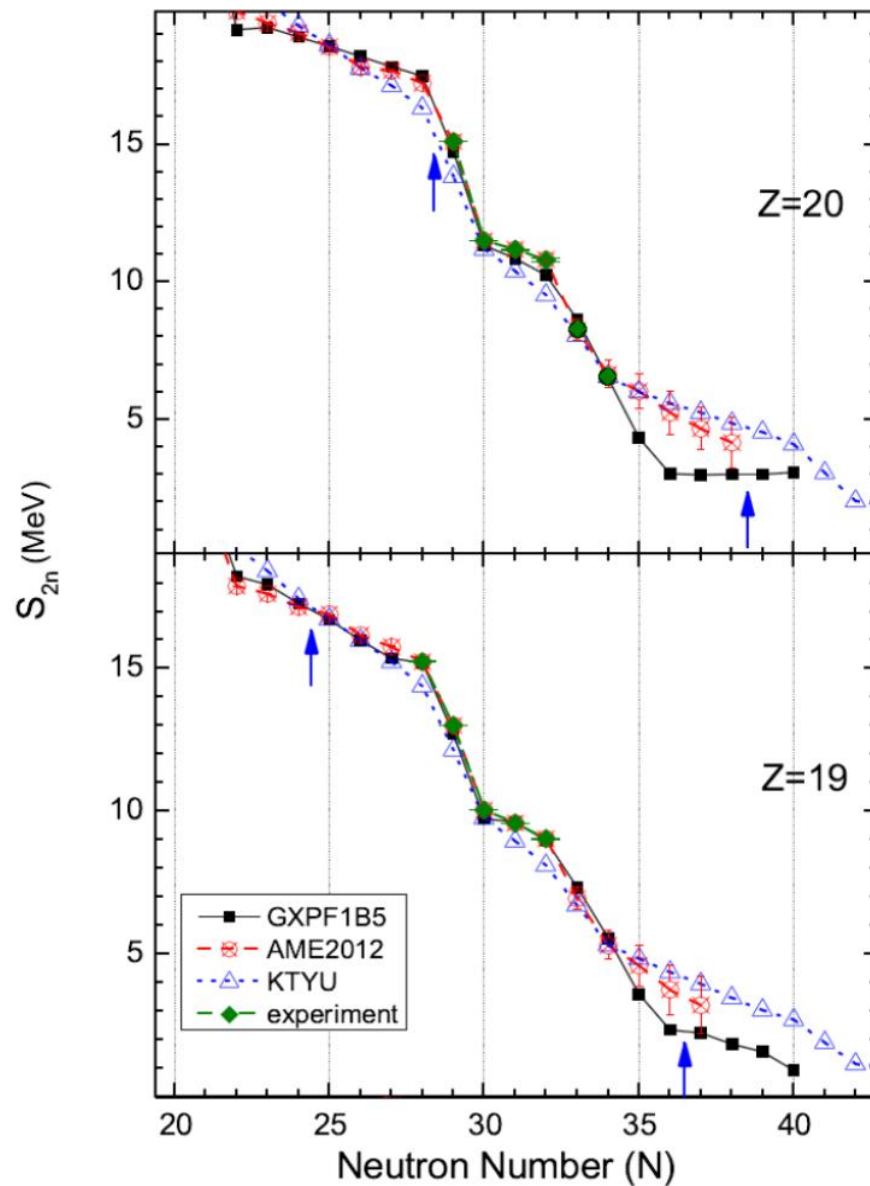
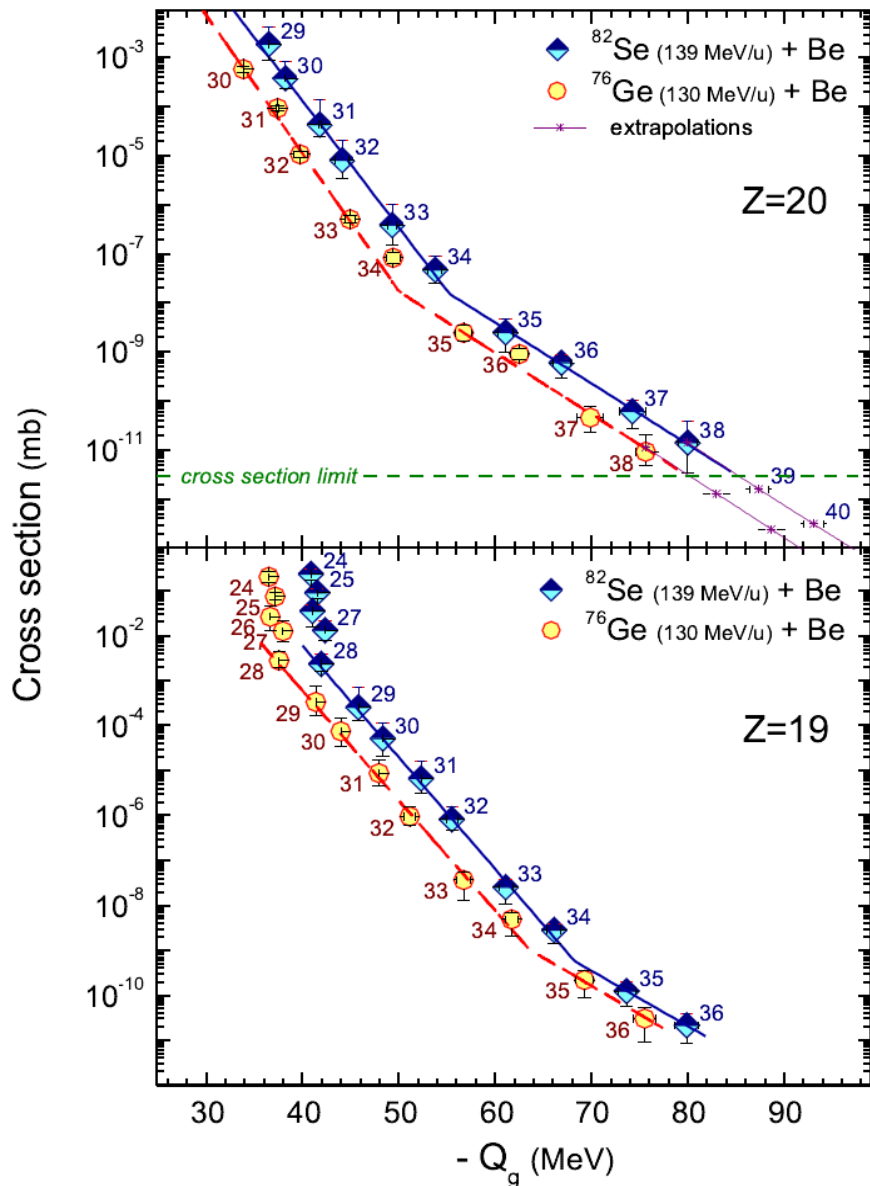
$N_W = 90, N_{Be} = 330, N_{Be_Integral} = 126$





**By product information
about W-target lifetime**





Experimental masses:

A.T. Gallant et al., Phys. Rev. Lett. 109, 032506 (2012)

F. Wienholtz et al., Nature 498 (2013) 346

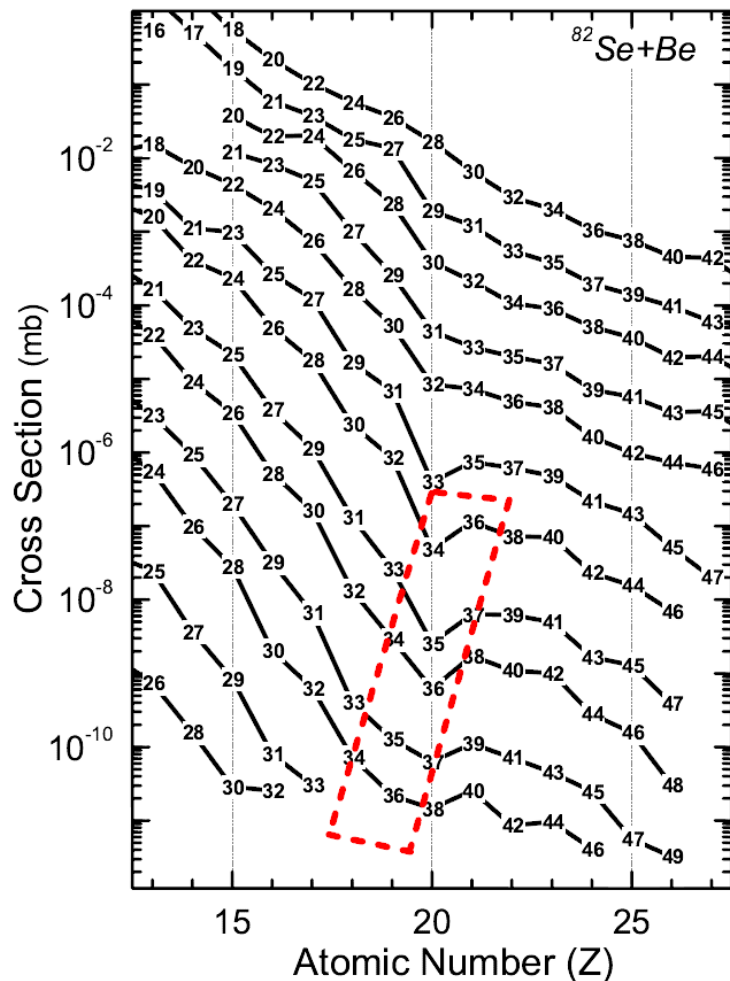


FIG. Production cross section versus atomic number (Z) for fragments from reaction of ^{82}Se with beryllium targets. Lines are connected according to constant $N - 2Z$, while labels represent the neutron number.

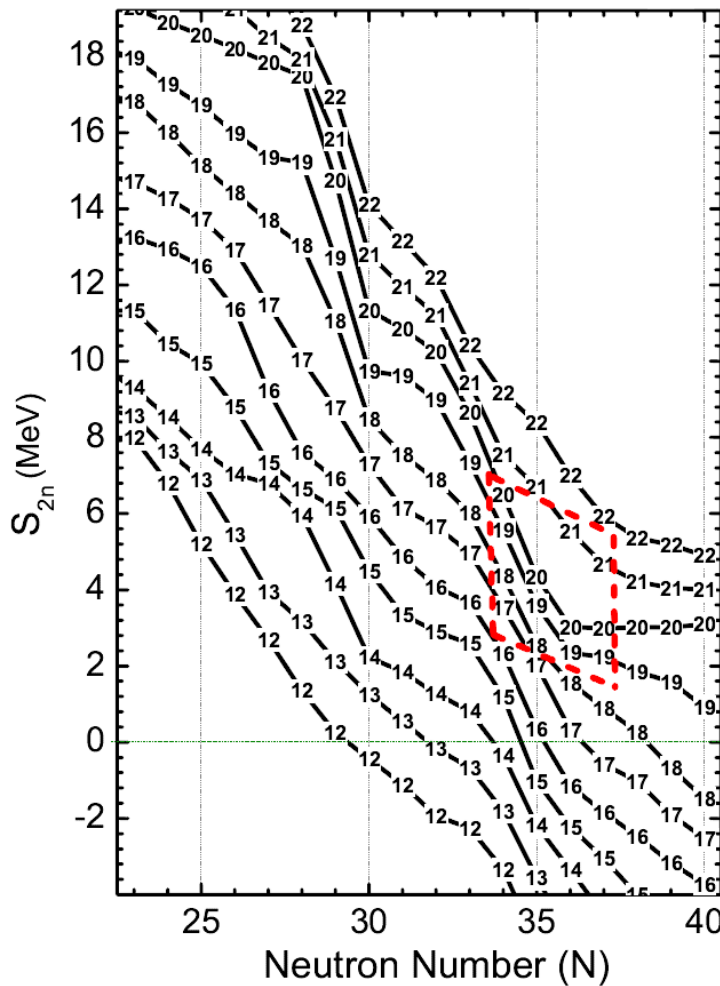
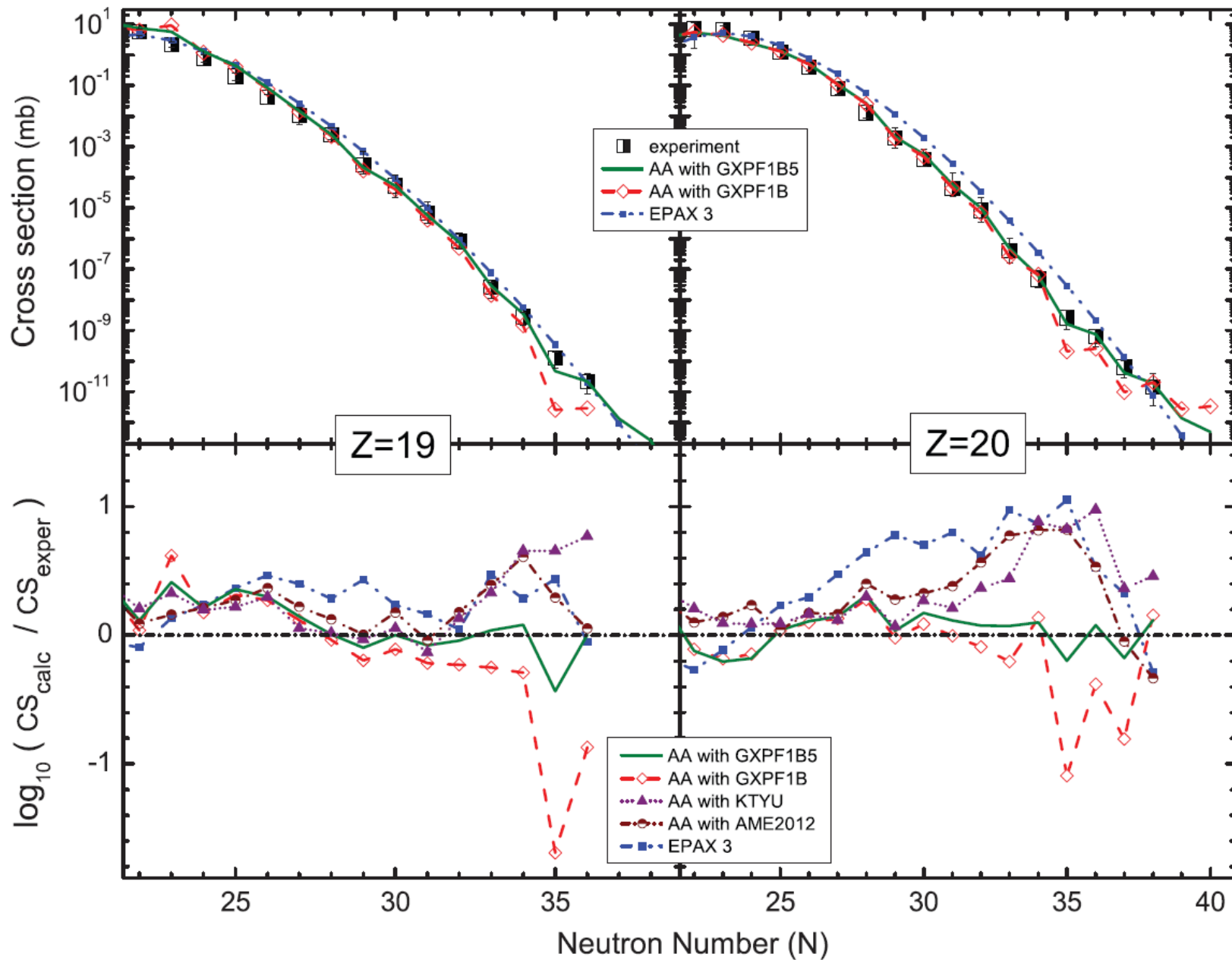


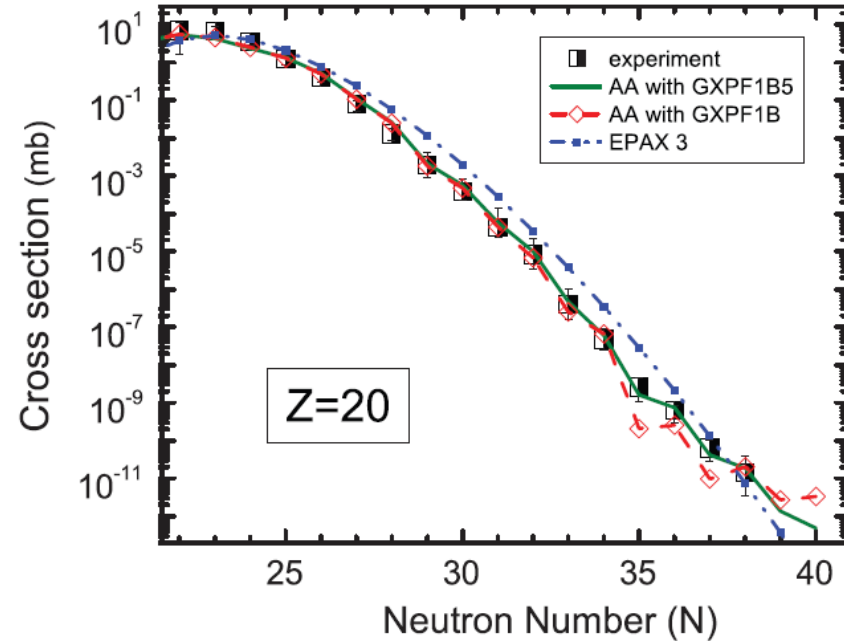
FIG. Two-neutron separation energy S_{2n} versus neutron number (N) for elements $12 \leq Z \leq 22$. Values are calculated using results from the GXPF1B5 model. Labels in the lines show atomic numbers of nuclei.

No such dump with other theoretical models



$$\sigma(^{60}\text{Ca})_{\text{estimation}} = 4(\pm 1) \times 10^{-16} \text{ b}$$

$$\sigma_{\text{lowest measured @ MSU}} = 3 \times 10^{-15} \text{ b}$$

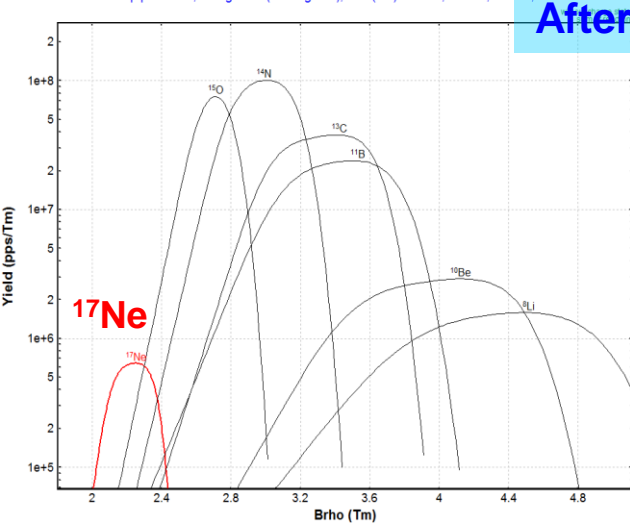


Primary beam	Estimation method	^{59}Ca cross section (mb)	^{60}Ca cross section (mb)
^{82}Se	AA	1.39e-12	4.83e-13
^{82}Se	Q_g	1.62e-12	3.19e-13
^{76}Ge	Q_g	1.36e-12	2.47e-13
^{82}Se	EPAX3	3.73e-13	1.65e-14
^{76}Ge	EPAX3	3.68e-13	1.71e-14

AA: Masses calculated with the GXPF1B5 interaction

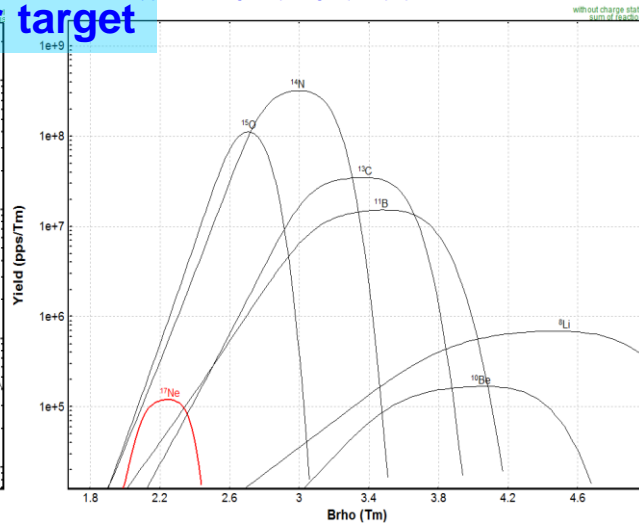
Stripper: Momentum OC

^{20}Ne (170.0 MeV/u) + Be (3196 mg/cm²); Settings on ^{17}Ne ; Config: DDSWDDSA
 dp/p=1.00%; Wedges: Al (150 mg/cm²); Brho(Tm): 2.2230, 2.2230, 2.1311, 2.1311



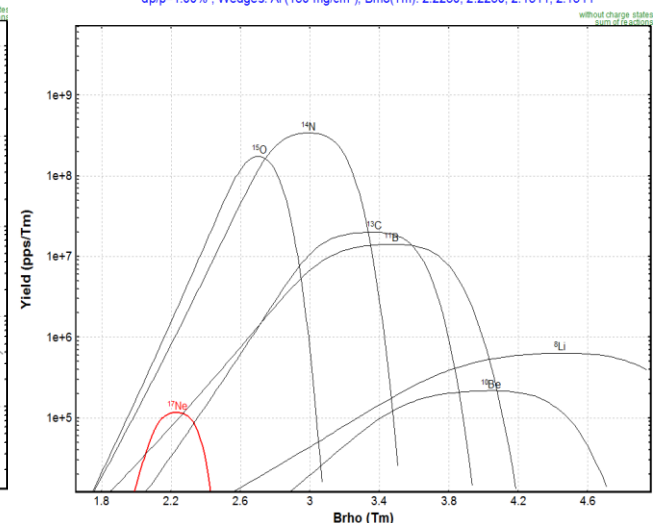
Stripper: Momentum OC

^{20}Ne (170.0 MeV/u) + Be (3196 mg/cm²); Settings on ^{17}Ne ; Config: DDSWDDSA
 dp/p=1.00%; Wedges: Al (150 mg/cm²); Brho(Tm): 2.2230, 2.2230, 2.1311, 2.1311



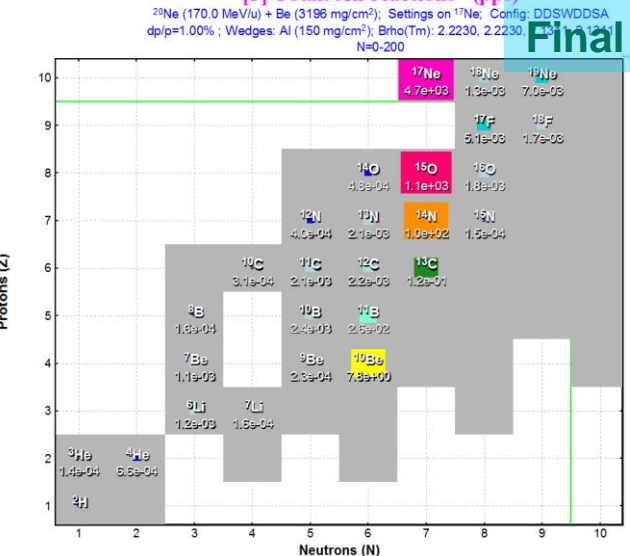
Stripper: Momentum OC

^{20}Ne (170.0 MeV/u) + Be (3196 mg/cm²); Settings on ^{17}Ne ; Config: DDSWDDSA
 dp/p=1.00%; Wedges: Al (150 mg/cm²); Brho(Tm): 2.2230, 2.2230, 2.1311, 2.1311



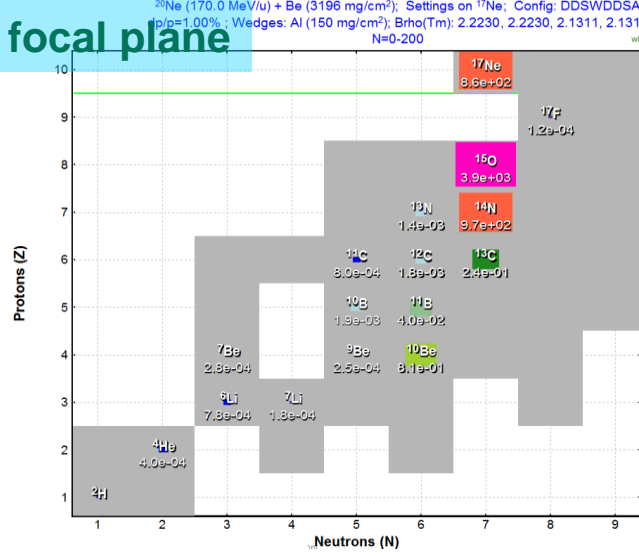
[3] Total: All reactions (pps)

^{20}Ne (170.0 MeV/u) + Be (3196 mg/cm²); Settings on ^{17}Ne ; Config: DDSWDDSA
 dp/p=1.00%; Wedges: Al (150 mg/cm²); Brho(Tm): 2.2230, 2.2230, 2.1311, 2.1311
 N=0-200



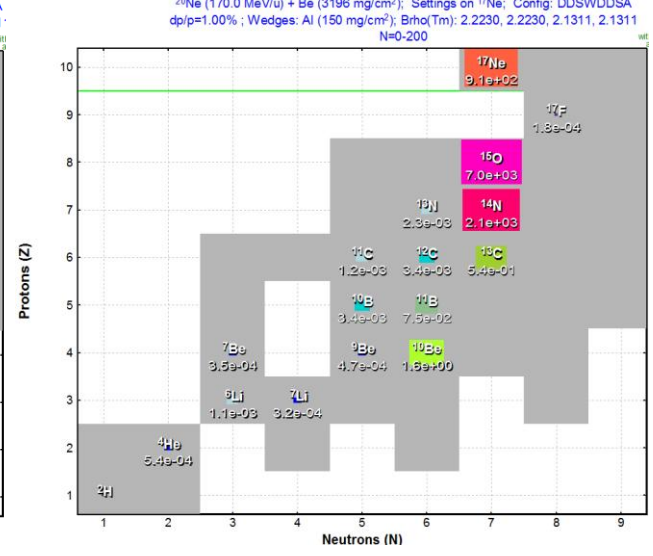
[3] Total: All reactions (pps)

^{20}Ne (170.0 MeV/u) + Be (3196 mg/cm²); Settings on ^{17}Ne ; Config: DDSWDDSA
 dp/p=1.00%; Wedges: Al (150 mg/cm²); Brho(Tm): 2.2230, 2.2230, 2.1311, 2.1311
 N=0-200



[3] Total: All reactions (pps)

^{20}Ne (170.0 MeV/u) + Be (3196 mg/cm²); Settings on ^{17}Ne ; Config: DDSWDDSA
 dp/p=1.00%; Wedges: Al (150 mg/cm²); Brho(Tm): 2.2230, 2.2230, 2.1311, 2.1311
 N=0-200



^{17}Ne / all
82%

Default settings:
EPAX3
UP #1, coef=3

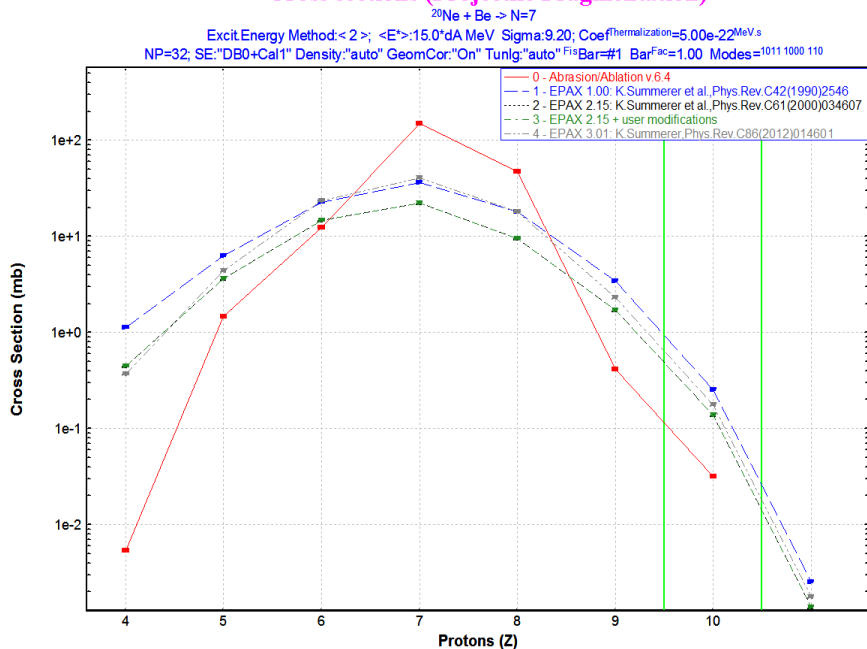
^{17}Ne / all
15%

settings:
AA (15/9.4)
UP #1, coef=3.5

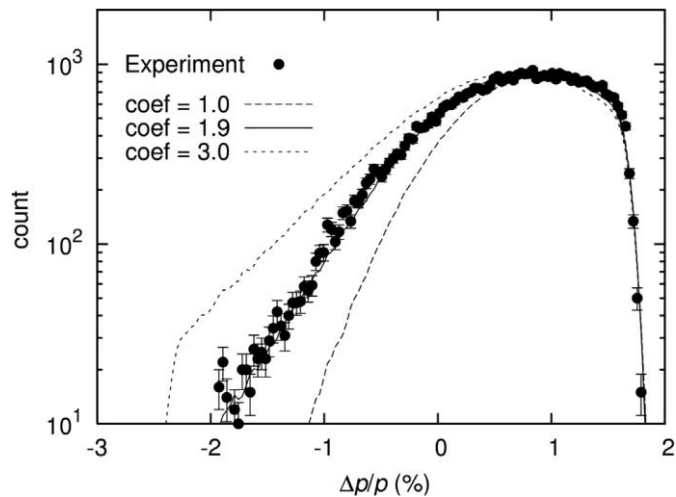
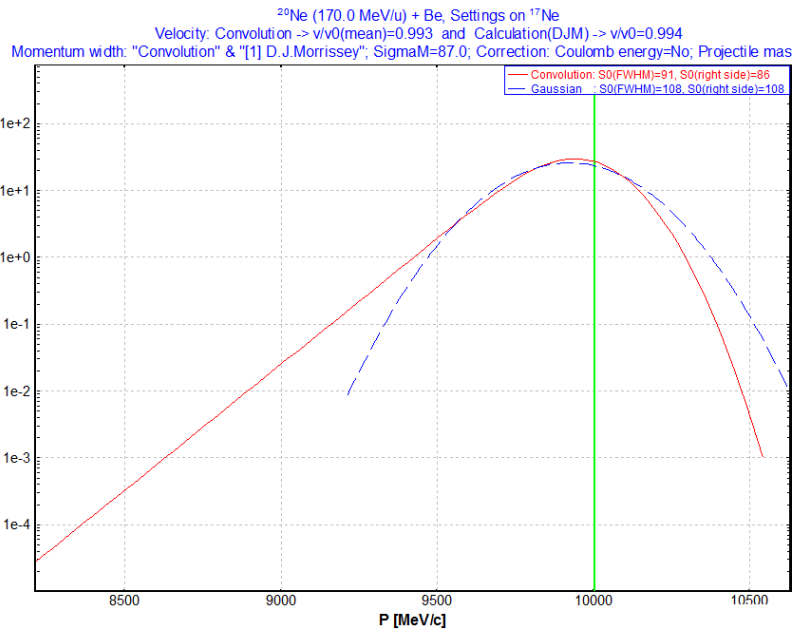
^{17}Ne / all
9%

settings:
AA (15/9.4)
UP #1, coef=4.0

Cross sections (Projectile Fragmentation)



Momentum distributions



Convolution of Gaussian (Fragmentation) and Exponent (Friction) distributions

$^{20}\text{Ne}(170.0 \text{ MeV/u}) + \text{Be} \rightarrow ^{17}\text{Ne}$

Settings for Gaussian distribution

$f(p) \approx \exp\left(\frac{p}{\tau}\right) \cdot \left[1 - \text{ferr}\left(\frac{p - p_0 + \frac{\sigma_{II}^2}{\tau} - \text{shift} \cdot \tau}{\sqrt{2} \sigma_{II}}\right) \right]$

$\sigma_{II}^2 = \left(\sigma_0^{\text{conv}} \sqrt{\beta_p}\right)^2 \frac{A_p^* (A_p - A_p^*)}{A_p - 1}$ $\tau = \frac{\text{coef}}{\beta} \sqrt{A_p^* E_s}$

Settings for convolution

Separation Energy	E_s	coef	shift	FWHM / 2.355 (°)	tau	P(Ymax)	peak	v/v_0 mean
<input type="radio"/> Energy from Qg	23.5	3.344	0.158	153.3	126.4	9928	0.995	0.992
<input checked="" type="radio"/> Excitation from dSurface	13.7	4	0.149	149.4	115.3	9934	0.995	0.993
<input type="radio"/> Qg + dSurface	37.2	2.936	0.153	156.6	139.6	9919	0.995	0.992

$\sigma_0^{\text{conv}} = 91.5 \text{ MeV/c}$
 $g = 0.95 \text{ MeV/tm}^2$ (*) - with Gamma-factor

Buttons: Plot 1D, Plot - Conv. Analysis, OK, Cancel, Help, Make default

Projectile $^{20}\text{Ne}^{10+}$
 53 MeV/u 1000 pA
Fragment $^{17}\text{Ne}^{10+}$

Target Be
 100 $\mu\text{g}/\text{cm}^2$

Stripper

D1 Brho
 1.6838 Tm
 -11 μ +11
 -50 μ +50

Wedge Be
 210 $\mu\text{g}/\text{cm}^2$

D2 Brho
 1.3685 Tm
 -5 μ +5
 -5 μ +5

M F3_PPAC Al
 3 $\mu\text{g}/\text{cm}^2$

S Drift beam-ne
 8.79 m
 -10 μ +10
 -10 μ +10

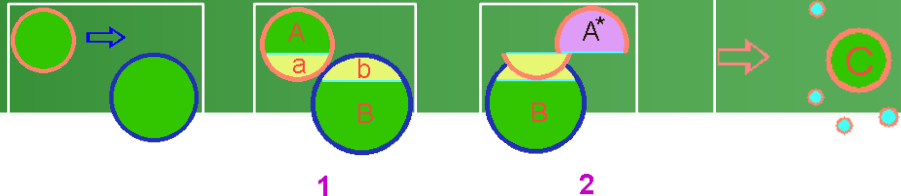
M F4_dE Si
 300 $\mu\text{g}/\text{cm}^2$

M F4_E Si
 10 μm

Config Acculina
 option A1900_2007
 version 8.4.1

EPD
 3.66%

Beam	Target	Reaction	Cross section	result
^{20}Ne	Be	EPAX2	1.39E-01	7.70E-01
^{20}Ne	Be	AA	6.43E-02	3.56E-01
^{20}Ne	Be	AA, Rt=7fm	4.03E-02	2.23E-01
^{20}Ne	Ni	EPAX2	2.43E-01	2.43E-01
^{20}Ne	Ni	AA, EE#0	1.68E+00	1.68E+00
^{24}Mg	Be	EPAX2	8.63E-02	4.78E-01
^{24}Mg	Be	AA	3.08E-02	1.71E-01
^{24}Mg	Ni	EPAX2	1.42E-01	1.42E-01
^{24}Mg	Ni	AA, EE#0	1.72E+00	1.72E+00
^{16}O	^3He	FR (20MeV/u)	6.00E-01	7.62E+00
^{20}Ne	^3He	FR	1.00E-02	1.27E-01
^{24}Mg	^3He	FR	4.00E-03	5.08E-02
^{24}Mg	^9Be	FR	2.00E-03	1.11E-02



3-step projectile fragmentation model

Process	Momentum distribution
1 Abrasion Removal of the part "a" (statistics)	Gaussian $\psi(p_{pf}) = \frac{1}{\sqrt{2\pi} \sigma_{pf}} \exp\left(-\frac{(p_{pf} - p_{0pf})^2}{2\sigma_{pf}^2}\right)$
2 Friction - loss of kinetic energy Transformation into the internal degrees of freedom. Exchange of nucleons	Exponential attenuation $\phi(p_1, p_2) = \frac{1}{\tau} \exp\left(-\frac{p_2 - p_1}{\tau}\right)$
3 Ablation light nuclei emission, gamma-emission	Broadening velocity peak maximum does not shift

$$f(p) = \phi \otimes \psi \cong \exp\left(\frac{p}{\tau}\right) \cdot \left[1 - ferr \left(\frac{p - p_0 + \frac{\sigma_{pf}^2}{\tau} - s \cdot \tau}{\sqrt{2} \sigma_{pf}} \right) \right]$$

Where $\tau = coef \cdot \sqrt{A_{PF} \cdot E_S} / \beta$, and

$$\sigma_{pf}^2 = \beta \sigma_0^2 \frac{A_{PF}(A_P - A_{PF})}{A_P - 1}$$

E_S is the energy spent to split the projectile (mass difference, surface energy excess)
 A_{PF} is the mass number of the prefragment. Three parameters to fit: σ_0 , s , $coef$.

Excitation Energy of prefragment

Prefragment

A	Element	Z	Table of Nuclides
17	Ne	10	

Beta+ decay

Reaction: 20Ne + Be

Excitation Energy in the code = 39.90 MeV

Models

- A. J.W.Wilson et al., NIM B18 (1987) 225-231
- B. J.-J.Gaimard and K.-H.Schmidt, NPA531 (1991) 709
- C. Parametrized Gaussian distribution

Use LISE++ corrections for Geometrical A-A model

Apply thermalization for Excitat. energy according to J.-J.Gaimard & K.-H.Schmidt, NPA531 (1991) 709; see Equation 3.4

Make default

Plot OK Cancel Help

Ap is the projectile mass
d_abr is the number of abraded nucleons

for model "C"

region "L"	< Z boundary = < or < A boundary = <	region "H"
------------	--	------------

A. J.W.Wilson, L.W.Townsend, F.F.Badavi, NIM B18 (1986) 225-231 -- geometrical model

Excitation Energy = 13.70 MeV gamma = 0.95 MeV/fm²

Standard deviation = 16.63 MeV sigma = 9.6 * d_abr^(0.5) [MeV]

$$E^* = (\gamma \cdot f \cdot \Delta S)_{geom} + E_{friction}$$

f- Correction factor of Surface distortion excitation

f = 1 + coef1 * d_abr / Ap + coef2 * (d_abr / Ap)²

c1 = 1.5 c2 = 2.5 f = 1.28

Excitation Energy Transfer (friction)

E_friction = coef1 * Cp + coef2 * Cp * Ct

Cp is the length of the longest chord in the projectile surface interface, Ct is the chord of intersection

coef1 = 6.5 Cp = 5.51 fm

coef2 = 0 Ct = 3.89 fm

Use Friction E_friction = [] MeV

B. J.-J.Gaimard and K.-H.Schmidt, NPA531 (1991) 709 -- convolution of triangle distributions

Hole depth (MeV) <E*> = 13.36 * d_abr [MeV] Mean Excitation Energy = 40.32 MeV

40 sigma = 9.43 * d_abr^(0.5) [MeV] Standard deviation = 15.87 MeV

C. Parametrized Gaussian distribution -- simplified combination of K.-H.Schmidt et al. NPA710 (2002) 157-179

do NOT use region "L" (as model "B") Mean Excitation Energy = 39.90 MeV

use Z to separate regions Standard deviation = 16.63 MeV

use A to separate regions

Region "L"		Region "H"	
< E*>	sigma	< E*>	sigma
0 * A ² +	0 * A +	0 * d_abr ² +	0 * d_abr +
3 * A +	2 * A ^(1/2) +	13.3 * d_abr +	9.6 * d_abr ^(1/2) +
0 [MeV]	0 [MeV]	0 [MeV]	0 [MeV]

Should be revision for excitation energy in the
"Universal parameterization"

September 10, 2006. 30 years of Projectile Fragmentation workshop, ACS

What do we know from experiments?

1. Decreasing the projectile velocity → increase of production cross-section of neutron-rich isotopes
2. Increasing target mass → increase of production cross-section of neutron-rich isotopes
3. Low Exponential tail in momentum distribution is due to dissipative processes

Why do cross-sections increase?

From the AA formalism:

Increasing excitation low-energy tail.

Broadening or/and shift of excitation energy distribution take place due to **friction?**

If assume dissipation processes it is possible to answer on preceding questions:

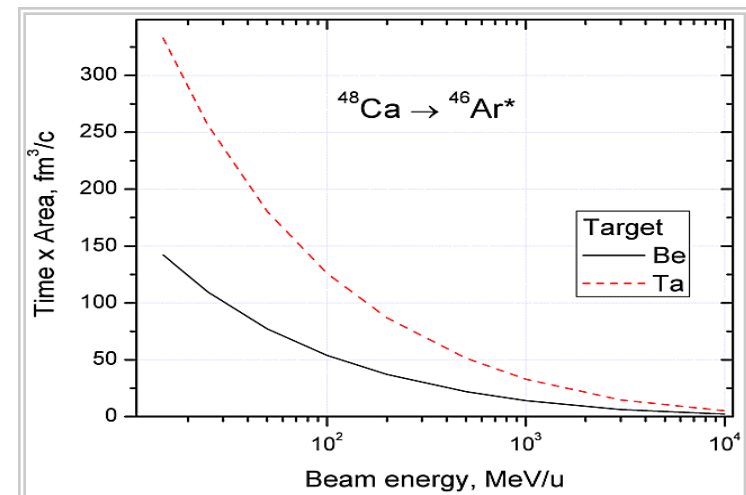
1. Dissipation Time is increasing
2. Dissipation Time and Touching Area are increasing due to target size

Time of dissipation ~ to beam velocity & Chord_max

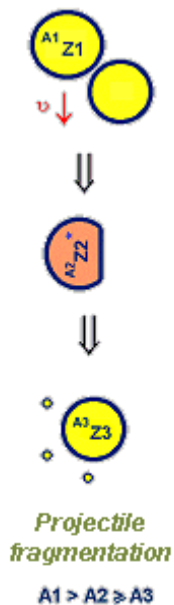
Touching area is ~ to Chord_min²

Target thermal capacity ~ target mass

$$dQ = -K \frac{dT}{dx} dS dt$$



EMIS. 24-29.06.07, Deaville, France

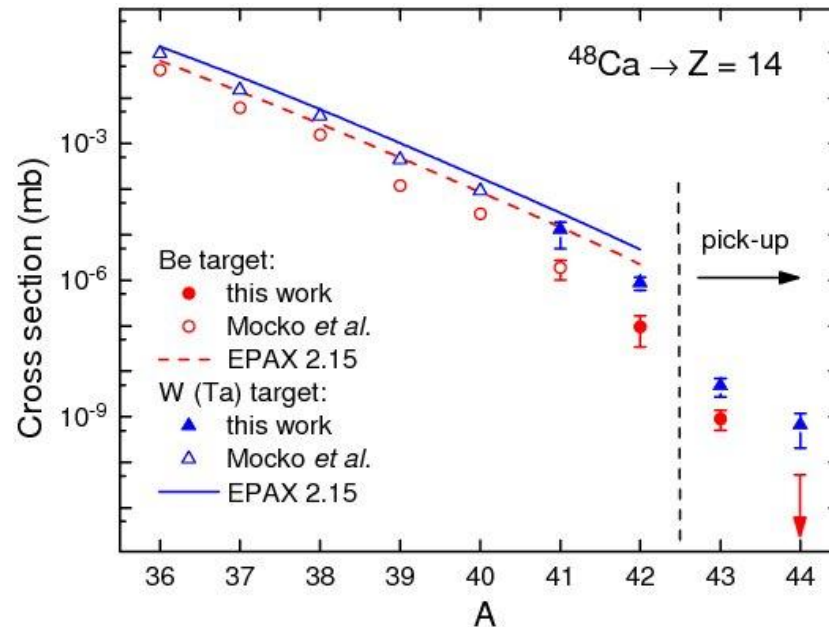


NSCL / MSU

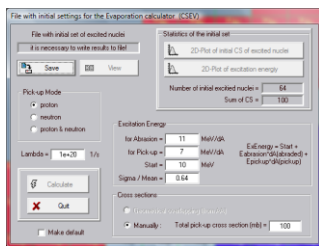
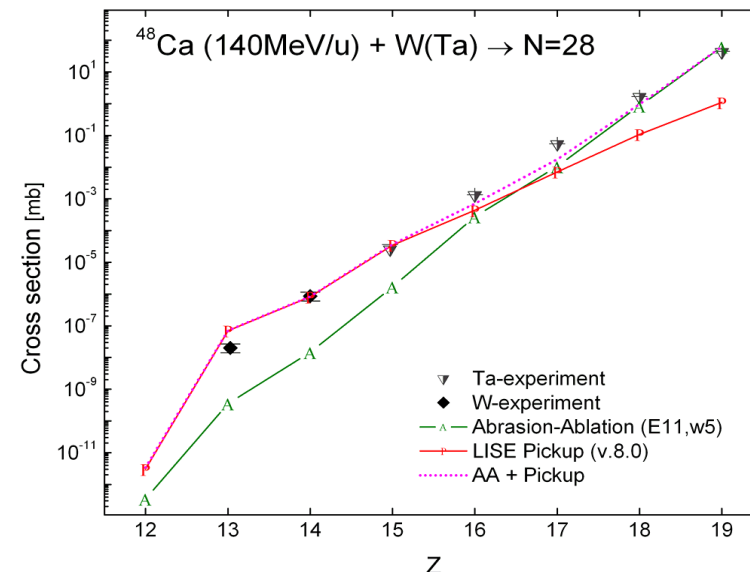
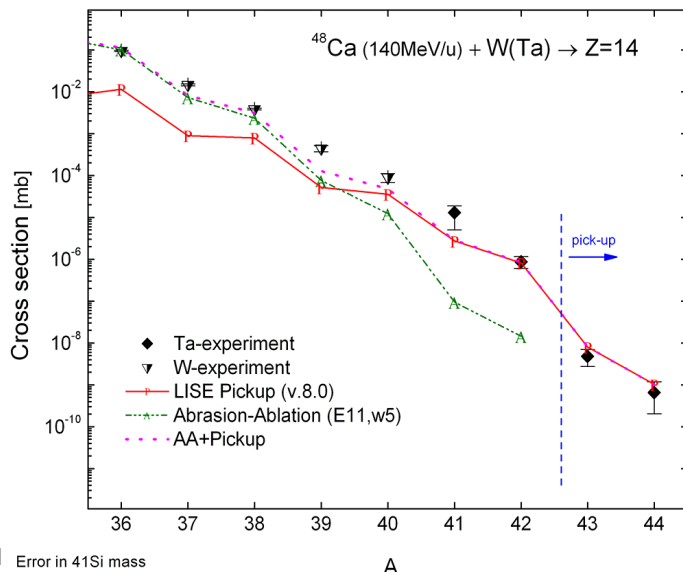
$^{40}\text{Mg}, ^{42,43}\text{Al}$ Nature 449 (2007) 1022

^{44}Si Phys. Rev. C 75, 064613 (2007)

LISE++ Abrasion-Ablation cannot explain production cross section dependences from target properties (size, N/Z ratio) and projectile energy. No explanation for pickup contribution



LISE++ Abrasion-Dissipation-Ablation model (ADA) /under construction/



Just ONE

Universal model for

cross sections and

momentum distributions

should be developed...

of the present study of fragmentation of ^{76}Ge and ^{82}Se beams ^{76}Ge

- New 15 neutron-rich isotopes ($17 \leq Z \leq 25$)
- Evidence for a Change in the Nuclear Mass Surface
- Cross sections and Momentum distributions
- A new approach to measure momentum distributions
- New parameters for DJM momentum distribution model

 ^{82}Se

- Isotopes ^{64}Ti , ^{67}V , ^{69}Cr , and ^{72}Mn were identified for the first time. One event was registered consistent with ^{70}Cr and another one with ^{75}Fe
- The momentum distributions of 126 neutron-rich isotopes of elements with $11 \leq Z \leq 32$ were measured and compared to models
- The cross sections for 330 nuclei produced by the ^{82}Se beam were measured
- The experiment confirmed the trend of our previous experiment using a ^{76}Ge beam, where the most neutron-rich nuclei of elements with $Z = 19$ to 21 have been produced with an enhanced rate compared to the Q_g systematics
- This result has been explained with a shell model that predicts a subshell closure at $N = 34$ and a more pronounced one at $Z = 20$
- The measured cross sections were best reproduced by LISE++ Abrasion-Ablation model using masses derived from the full pf shell-model space with the GXPF1B5
- The cross section for production of ^{60}Ca using a ^{82}Se beam on beryllium has been estimated at $4(\pm 1) \times 10^{-16} \text{ b}$

This work was supported by NSF No. PHY-06-06007, PHY-06-06007, No. PHY-10-68217, and No. PHY-11-02511 grants.